

Exploring Rate of Descent

Rate of Climb = ROC = dh/dt

h = altitude

$$\text{ROC} = V_T \sin(\gamma) \quad [1]$$

$$dV_T/dt = g [(T-D)/W - \sin(\gamma)] \quad [2]$$

$$dV_T/dt = dV_T/dh * dh/dt = dV_T/dh * \text{ROC} \quad [3]$$

substituting [3] into [2]

$$dV_T/dh * \text{ROC} = g [(T-D)/W - \sin(\gamma)] \quad [4]$$

substituting [1] into [4]

$$V_T * dV_T/dh * \text{ROC} = g [(T-D)/W - \text{ROC}] \quad [5]$$

Rearranging

$$\text{ROC} = g [V_T * (T-D)/W] / [1 + V_T/g * dV_T/dh] \quad [6]$$

Unaccelerated Climb

$$\text{ROC} = V_T [(T-D)/W] \quad [7]$$

Rate of Descent = ROD = - ROC

$$\text{Drag} = 0.5 \rho C_D S V_T^2 \quad [8]$$

$$C_D = k C_L^2 \quad [9]$$

$$\text{Lift} = 0.5 \rho C_L S V_T^2 \quad [10]$$

When Lift = Weight

$$\text{Lift} = \text{Weight} = 0.5 \rho C_L S V_T^2$$

$$C_L = W / (0.5 \rho S V_T^2) \quad [11]$$

Drag = $1/8 k W^2 / (\rho S V_T^2)$ == very small number

$$\text{ROD} = V_T (D - T)/W \quad [12]$$

W^2 in Drag term has the effect of **decreasing** ROD as weight **increases**

Effect of Weight on ROD

K = 0.1

P = 0.002 slugs per cubic foot

V = 634 fps (= 0.6 Mach)

S = 1000 ft²

CL = 0.3554

D = 5965 lbs

W = 100,000 lbs

T = -500 lbs (at idle thrust in descent)

ROD = 46.9 fps = 22817 fpm

Weight (lbs)	ROD (fpm)
80,000	3,312
90,000	3,029
100,000	2,817
120,000	2,655

As weight increases, ROD decreases. (Note: Gliders T = 0, Gliders carry ballast weight to improve performance over long-distance trips)