

# **Brief Tutorial on Aircraft Propulsion**

**GMU SYST 460/560**

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**Prof. George Donohue**

# Overview

- **One of the most sophisticated of modern engineering designs**
- **Requires an understanding of Thermodynamics, Heat Transfer, Fluid Mechanics, Mechanics of Materials**
- **Designs have evolved from Prop to Jet, to Turbojet, Turboprop, High Bypass Ratio Fan Jet engines**

# Archimedes of Syracuse

## (c.287-212 BCE)

- **Sum of the Forces  $F = 0$**
- **Sum of the Moments  $(F \times L) = 0$**
- **Buoyancy force = weight of displaced fluid**
- **First Description of the Screw Propeller**
- **Foundation for Lighter than Air Flight in 18<sup>th</sup> cent.**
- *Pi: “The ratio of the circumference of any circle to its diameter is less than  $3 \frac{1}{7}$  but greater than  $3 \frac{10}{71}$ .” – calculus like derivation*
- **Great Mathematician and Military Engineer killed in 2<sup>nd</sup> Punic War**

# Leonardo da Vinci

(c. 1452-1519 CE)

- **Self Educated**
- **Continuity Equation**
  - $A_1 v_1 = A_2 v_2$ .
- **Precursor to “Conservation of Mass” and Bernoulli Equation in the 18<sup>th</sup> century**
- **Artist and Military Engineer**
- **Designs poorly documented**
- **Art works better known**
- **Conceptual Designs of Winged Gliders**

# Robert Boyle (1627-1691 CE)

- **$pV = \text{constant}$**
- **addition of temperature (T) in Charles's law**
  - **$pV/T = \text{constant}$  (Gas Law)**
- **Thermodynamic Equation of State**
  - **Used in Mechanical , Aerospace and Chemical Engineering**
- **Fundamental to understanding Brayton Cycle**
- **Foundation for Lighter than Air flight in 18<sup>th</sup> century**

# Isaac Newton (1642-1727 CE)

- **Great Mathematician, Physicist**
  - Vector Calculus
- **Law of Gravity**
- **Vector Relationships**
- **Conservation of Momentum**
- **$m\underline{v} = \text{constant}$**
- **$\underline{F} = m\underline{a} = d(m\underline{v})/dt$**
- **$\Sigma \underline{F} = 0$**
- *“If I have seen further, it is by standing on the shoulders of Giants”*

# Gottfried Wilhelm Leibniz (1646-1716 CE)

- **Great Statesman, Mathematician, Physicist**
  - Calculus
- **Altitude + *Vis Viva* ( $mv^2$ ) = Constant**
- **Today, we state this as the:**
  - “Law of Conservation of Energy” for solid bodies:
  - **Potential Energy + Kinetic Energy = Constant**

# Daniel Bernoulli (1700-1782 CE)

- Recognized Leibniz *vis viva* applied to fluid motion as well
- Medical experimentalist and Mathematician
- **Pressure +  $\rho v^2 = \text{Constant}$** 
  - Where  $\rho$  is the fluid density and  $v$  is the fluid velocity magnitude (along a streamline).
- Simple Equation to calculate both Airfoil Lift and Propeller/Fan Thrust



# Rudolf Julius Emanuel Clausius

## (1822-1888)

- The net change in the total energy of the universe is zero – **1<sup>st</sup> Law of Thermodynamics**
- For a thermodynamic cycle, the net heat supplied to the system equals the net work done by the system.
- Carnot efficiency =  $1 - \frac{\text{Low Absolute Temperature}}{\text{High Absolute Temperature}} < 100\%$
- The net change in the total entropy of the universe is always greater than zero – **2<sup>nd</sup> Law of Thermodynamics**
  - Temperature is a Measure of Entropy in a Heat Engine
  - $d(Q) = T d(S)$
- *Perpetual Motion Machine is impossible and the Universe is running down, Information order decays*

**John Barber (1734-1801)**  
**George Brayton (1830-1892)**  
**Frank Whittle (1907-1996)**

- **John Barber- UK pat. No. 1833 gas turbine engine**
  - **Materials inadequate to construction & operation**
- **George Brayton – US pat. (1872) constant pressure combustion thermodynamic cycle**
  - **Lost ground trans. Competition to Otto Cycle**
- **Air Commodore Sir Frank Whittle (RAF)**
  - **pat. (1930) Turbojet engine**
  - **Ranked by BBC poll #42 of 100 Greatest Britons**

# **Fundamental Attributes of All Aircraft Designs**

- **Aero 101:**
  - **If it Fly's, It weights TOO MUCH!**
- **Wright Bros Major Accomplishment:**
  - **Designed a System with Adequate Thrust to Drag ratio, Low weight with Adequate Structural Strength, Wings with Adequate Lift to Weight ratio and a Stable Flight Control system**

# Some Energy Density Comps

| Energy Storage Medium  | Energy Density (KW-Hr/Lb) |
|--|---------------------------|
| Lead-acid Auto Battery                                       | 0.016                     |
| CNG (CH <sub>4</sub> )                                       | 1.3                       |
| Gasoline (C <sub>8</sub> H <sub>18</sub> )                   | 5.3                       |
| Diesel (Kerosene or JetA) (C <sub>12</sub> H <sub>26</sub> ) | 5.8                       |

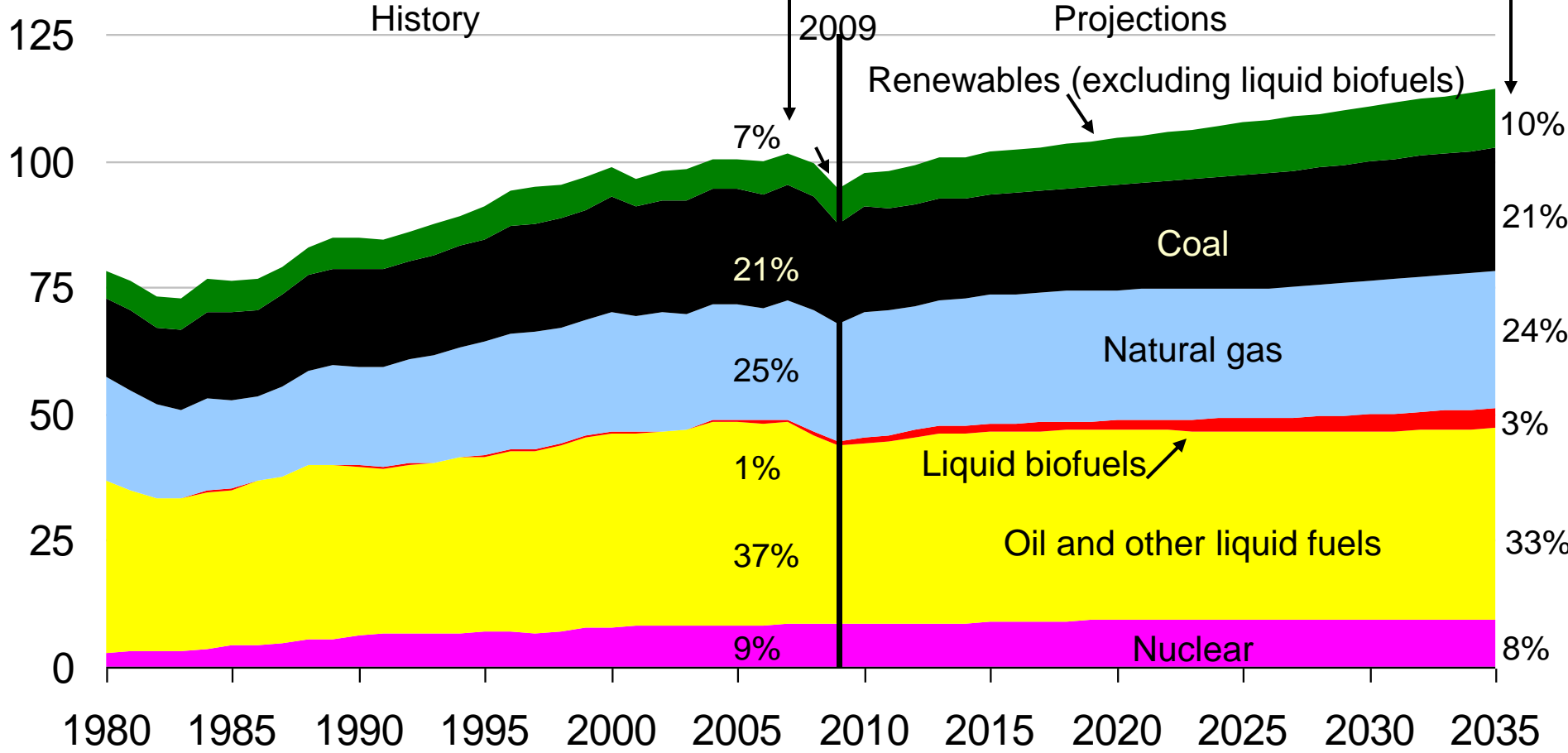
**TNT = 0.34**

**Natural Gas = CH<sub>4</sub> can be chained as (C<sub>n</sub>H<sub>2n+2</sub>)**



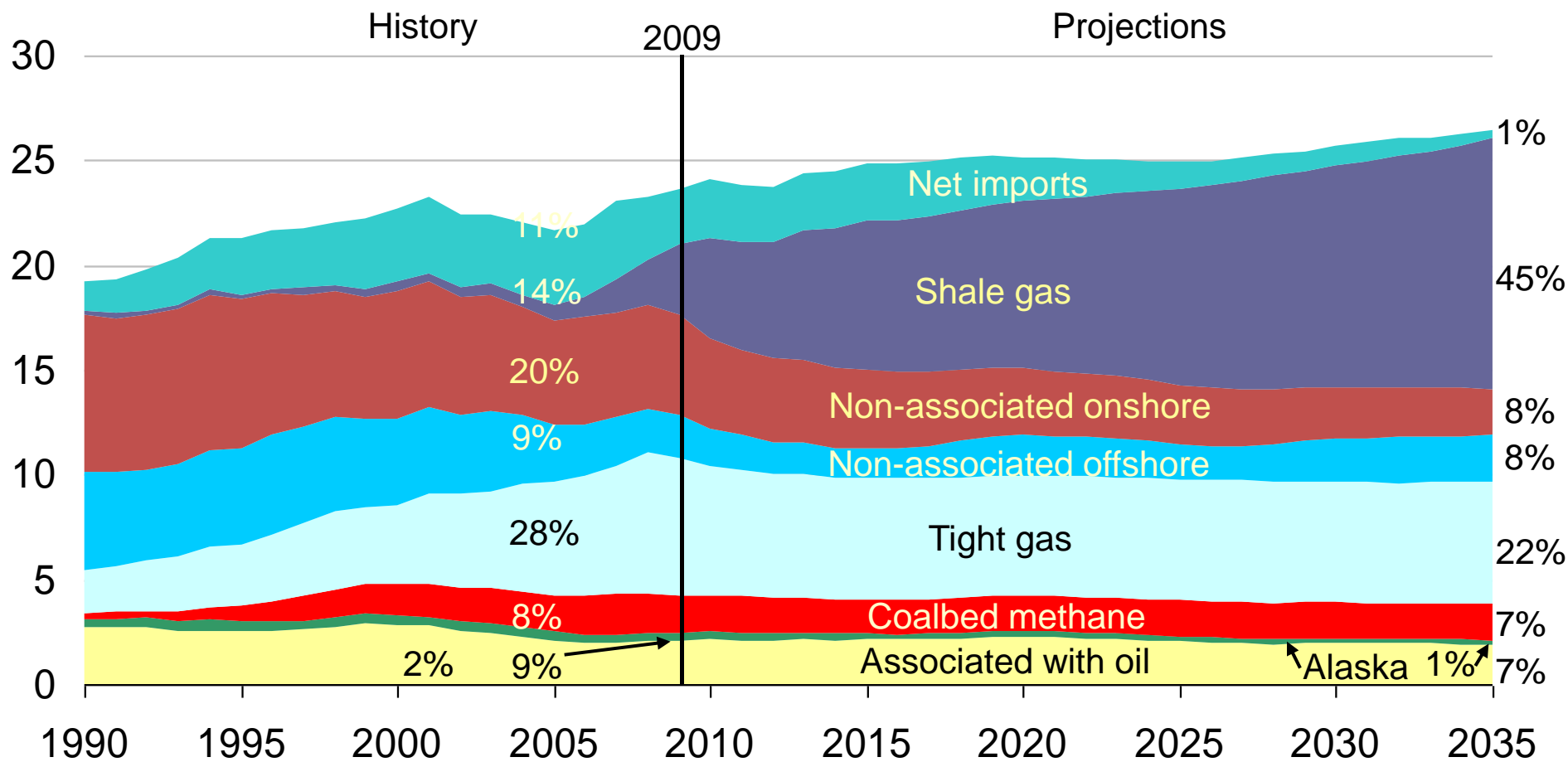
# Prediction: Renewables grow rapidly, but under current policies fossil fuels still provide 78% of U.S. energy use in 2035

U.S. primary energy consumption  
quadrillion Btu per year



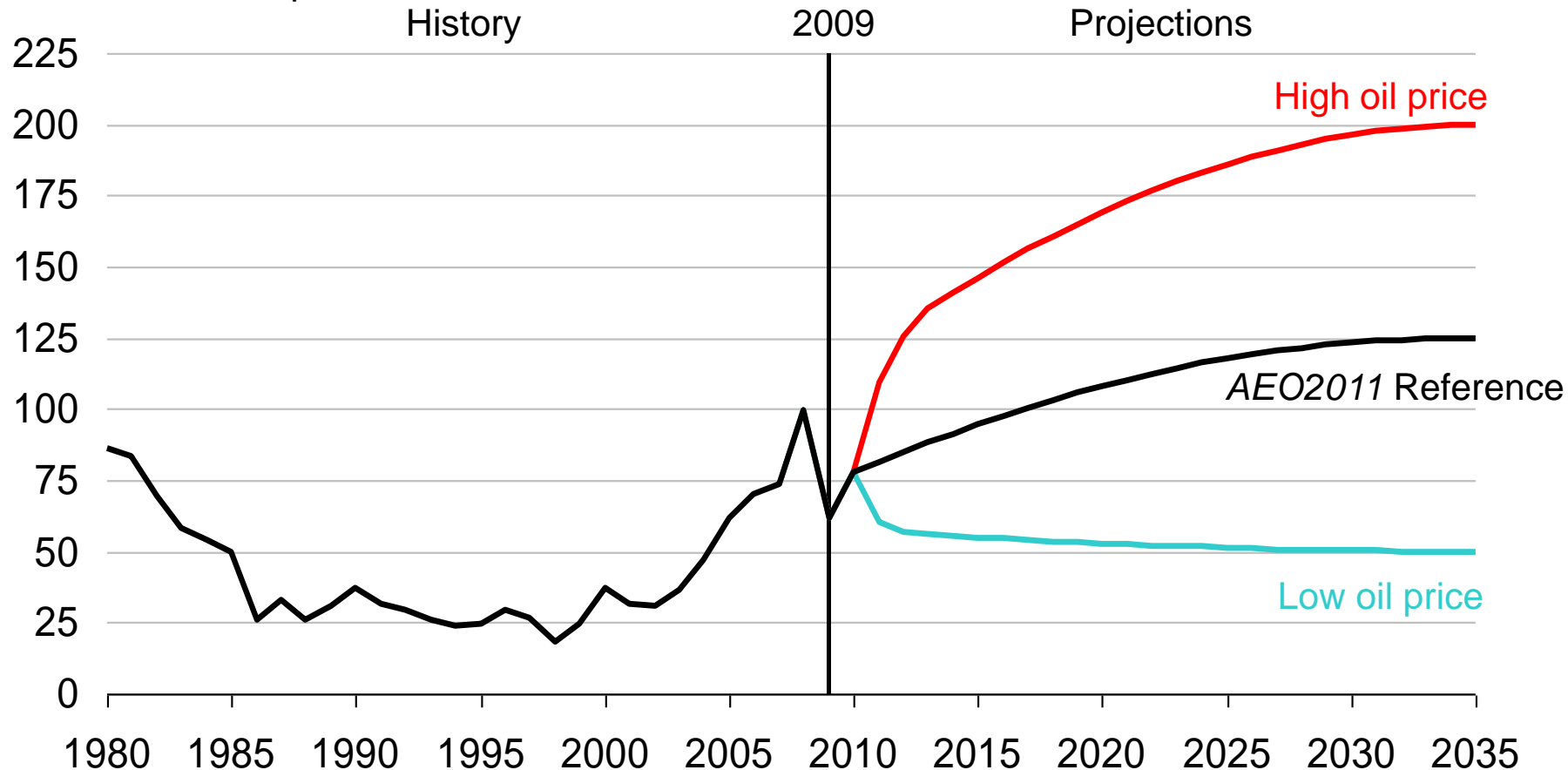
# Shale gas offsets declines in other U.S. supply to meet consumption growth and lower import needs

U.S. dry gas  
trillion cubic feet per year



# Oil prices in the *AEO2011* Report Reference Case rise steadily

annual average price of low sulfur crude oil  
real 2009 dollars per barrel



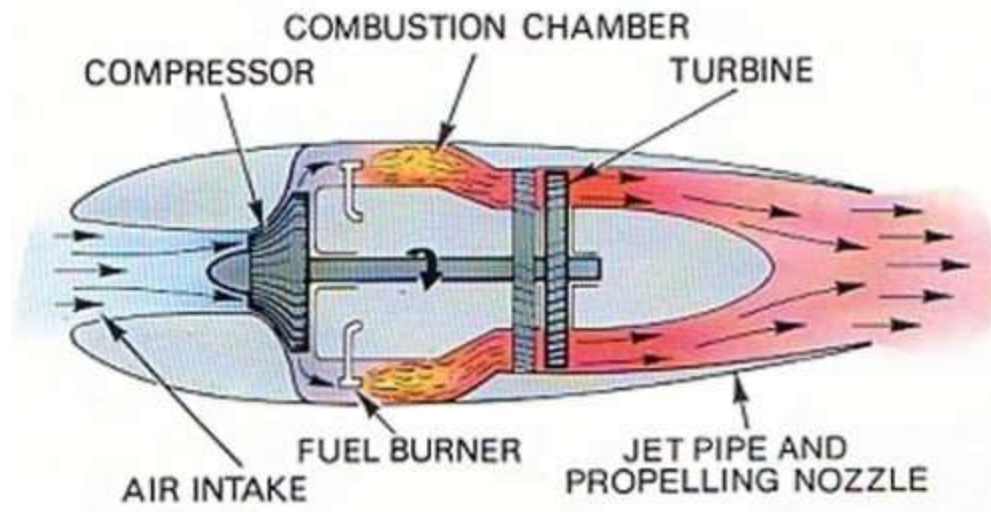
# Turbo Jet Fundamental Operating Principles

- **Suck -Air Intake**
- **Squeeze -Cool Axial Compression (Work In)**
- **Bang -Fuel + Combustion (Heat In)**
- **Blow -Hot Turbine to Extract (work Out)**
  
- **Thrust =  $d(m\underline{v})/dt$**



# Basic Axial Flow Turbo Jet Engine

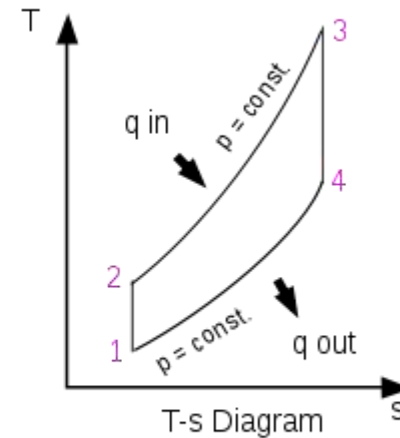
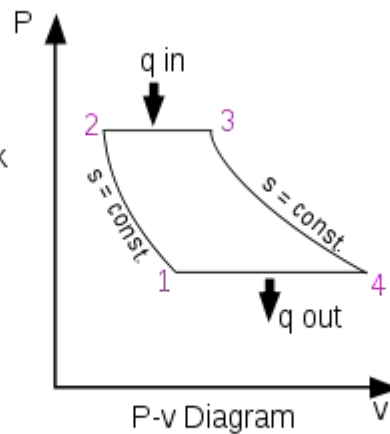
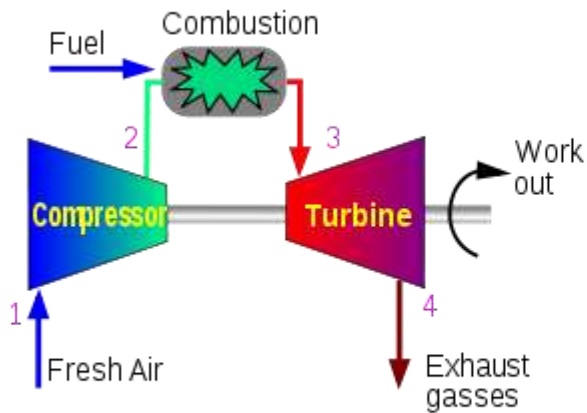
- **Low Mass Flow, High Exit velocity (~3:1)**
- **Low Efficiency**



# Brayton Cycle Thermodynamics

Actual Brayton cycle:

- [adiabatic process](#) - compression.
- isobaric process - heat addition.
- adiabatic process - expansion.
- isobaric process - heat rejection.



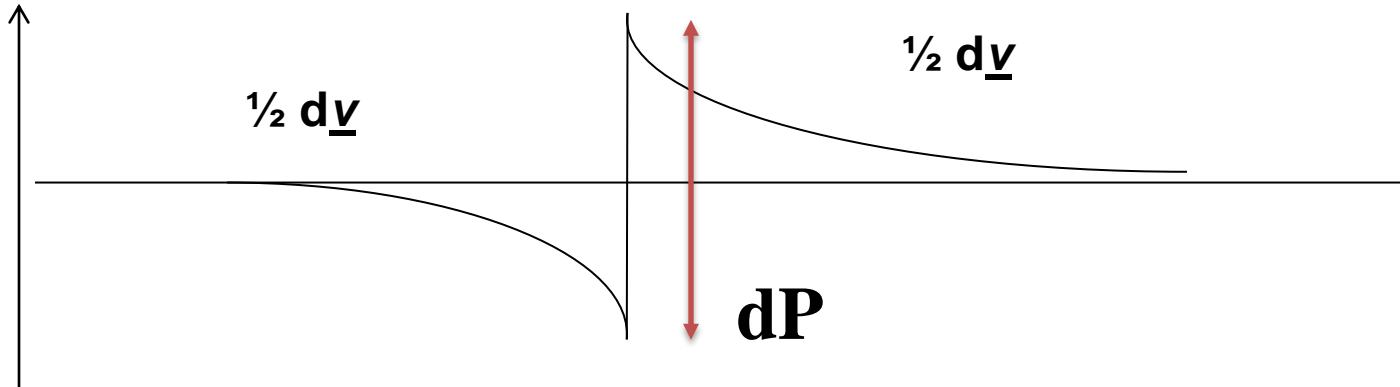
## Idealized Brayton cycle

$$\text{Carnot Eff.} = 1 - T_{\text{low}} / T_{\text{high}}$$

# Fan/Prop. Thrust & Power

- **Conservation of Energy – Bernoulli Equ. To find Pressure and Velocity Before & After Prop or Fan**
- **Thrust Force =  $d(m\underline{v})/dt$**
- **Useful Power =  $F_{\text{Thrust}} * \text{Velocity} = d(m\underline{v})/dt * \underline{v}$**
- **Power Input =  $dm/dt * \underline{v} * d\underline{v} [ 1 - d\underline{v}/2\underline{v} ]$**

**Pressure**



**Fuel + Heat = Work + Waste Heat**

# Est. of Max efficiency

- **Brayton Cycle Thermal (Carnot) Efficiency**
- **=  $1 - T_{\text{low}}/T_{\text{high}} = 1 - 300\text{K}(80\text{F})/1500\text{K}(2240\text{F}) \sim 80\%$  max**
  - **Increase Turbine Inlet Temp to Increase efficiency**
  - **Material Properties Limitation**
- **Fan (Prop) Propulsive Efficiency = Power Out/Power In**
  - =  $1 - d\underline{v}/2\underline{v} \sim 80\%$  max**
    - **Where Advance ratio (J) =  $\underline{v}/nD \sim 0.9$**
    - **D = Prop Disc Diameter**
    - **Bernoulli Equation (const. energy analysis along an accel. streamline)**
  - **Max Thrust at High  $d\underline{v}$**
  - **Max Efficiency at LOW  $d\underline{v}$**
- **Increase Mass Flow at Minimum  $d\underline{v}$  to Increase Thrust @ min. Wake Loss**
- **Combined Efficiency = Prop Eff. X Thermal Eff.**
  - $\sim 0.8 \times 0.8 \sim 0.64 \text{ MAX}$**

# Constraints

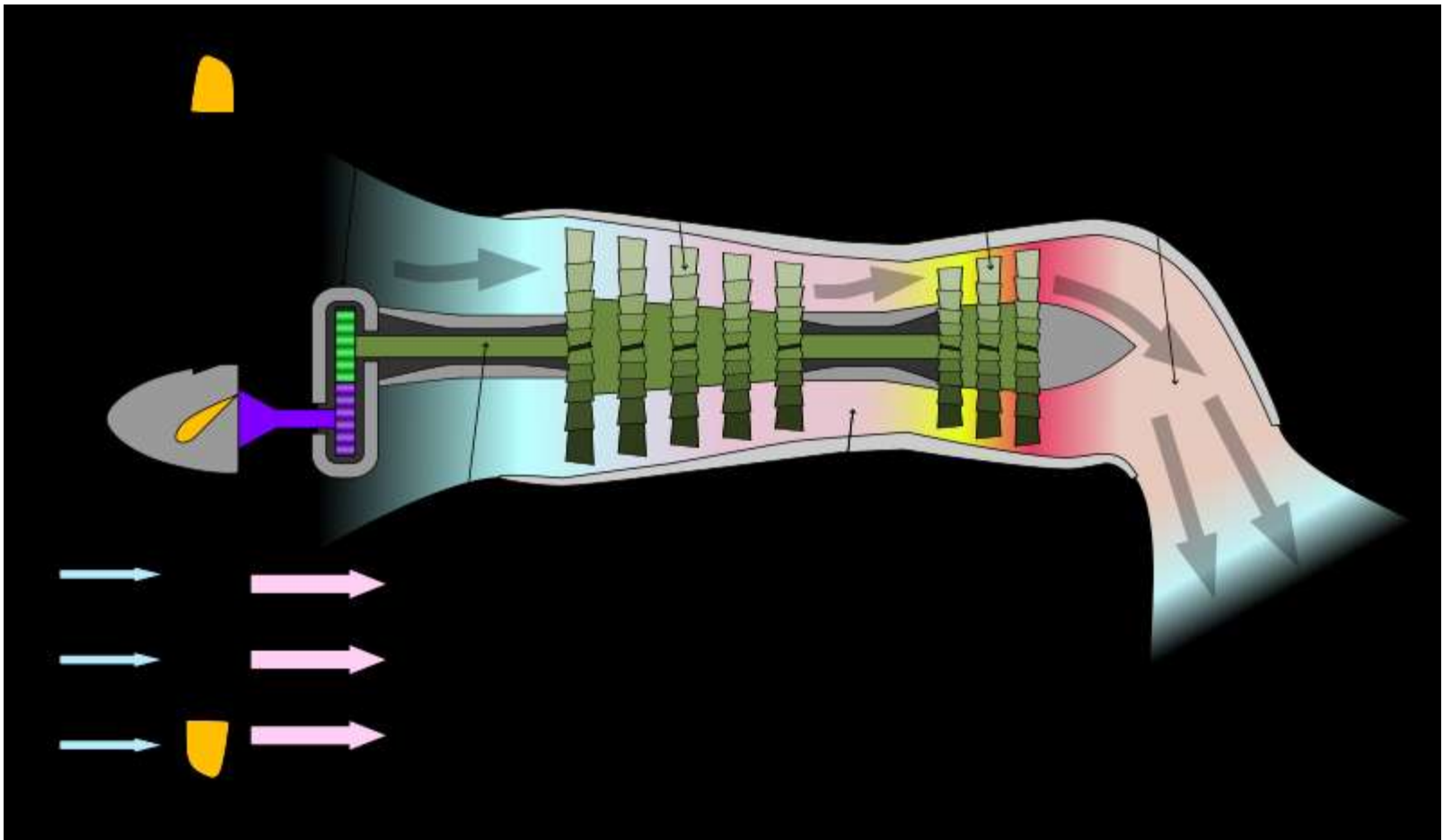
- **Prop/Fan Diameter**
  - **Tip Speed less than M1.0 (Noise/Drag)**
- **Advance Ratio (J)**
  - **Too High leads to Compressor Blade Stall**
- **Turbine Inlet Temperature**
  - **Too high leads to loss of Blade material strength**
    - **Active Cooling, Titanium, Ceramics**

# Specific fuel Consumption

## Lb Fuel/Hr/ Lb. Thrust

- **Turboprop = SFC  $\sim 0.5 * \underline{v}/550 * \text{prop. Eff (per shp)}$** 
  - Prop. Eff.  $\sim 0.8$
  - $\underline{V}$  (ft/sec)
  - $d\underline{v} \sim 1.5:1$
  - SFC @ 550 ft/sec  $\sim 0.40 / \text{Hr. @ } \sim M0.7$
- **Jets @ cruise = SFC  $\sim 0.9e^{(-0.05BPR)}$  :  $0 < BPR < 6.0$** 
  - Turbojet ( $d\underline{v} \sim 3:1$ )  $\sim 0.9$  lb fuel/hr / lb Thrust
  - LBPR Turbofan (BPR  $\sim 6$ )  $\sim 0.67$  lb fuel/hr / lb Thrust
  - HBPR Turbofan ( $\sim$ BPR 9:1)  $\sim 0.57$  lb fuel/hr/ lb Thrust
- **Max Combustion Efficiency @ “stoichiometric”**
  - Air/fuel 15:1 Turbine Inlet Temp TOO HIGH for Material strength
  - Air/fuel @ 60:1 Turbine Inlet temps ( 2,000 to 2,500 deg. F)

# Turbo Prop Vel $< M0.75$ with Controllable Pitch Propellers



# Some Typ. Turboprops

| A/C           | Engine       | TO rating (KW) | Weight (Kg) | Power/Weight |
|---------------|--------------|----------------|-------------|--------------|
| ATR-72-200    | PW 127       | 2,051          | 481         | 4.3          |
| C-130J        | RR AE 2100   | 3,424          | 702         | 4.9          |
| Dash 8 (Q400) | PW 150A      | 3,781          | 690         | 5.5          |
| Airbus A400M  | EU TP-400-D6 | 8,203          | 1,900       | 4.4          |
| TU-95 Bear    | NK-12MV      | 11,033         | 1,900       | 5.8          |

- **First applications in 1948**



# **Tu-95 w/ NK-12MV & (2) AV-6H CR Controllable Pitch Props**



# **TU-95 Bear Bomber (1952-present)**

## **TU-114 Pax Aircraft (1961-1991)**

- **Max Speed = 470 Kn**
- **Cruise Speed = 415 Kn**
- **Range = 3,300 nm**
- **Cruise Altitude = 26,000 ft.**
- **Service Ceiling = 39,000 ft.**
- **High Reliability**
- **224 PAX**
- **Pwr/Wt = 5.8 Kw/Kg**
- **Contra-Rotation Prop ~ 10% increased Efficiency**
- **4 X 4 Props Noisy (5X3 Scimitar would be a better combination)**

# Dash 8 (Q400)

- **Bombardier Aerospace**
- **Production (1983-pres)**
- **1,054 (Oct. 2011)**
- **\$27M price**
- **PW 150A engines**
- **$Pwr/Wt = 5.5 \text{ Kw/Kg}$**
- **78 PAX**
- **360 Knot Cruise**
- **27,000 Max Alt.**
- **1,500 nmi. Range**
- **Active Noise & Vibration Reduction (ANVS)**



# GE-Dowty R391, Prop (Q400)

- **P&W150A**
- **3,781 KW Take Off Pwr**
- **Carbon Fiber**
- **6 Blade**
- **Controllable pitch**
- **Scimitar Propellers**



# Antonov An-70

## Progress D-27 Propfan w/ SV27

### Contra-Rotation Scimitar Propellers

- **Dev. ~ 1992 - 1994**
- **14,000 shp**
- **Prop. Dia. 4.2m (165 in.)**
- **Wt. 1,650 Kg (3,600 lb.)**
- **Pwr/Wt = 6.3 Kw/Kg**
- **Never entered production**
- **Competitor to A400M**
- **High efficiency**
- **Noise Concerns**



# A400M

- **IOC ~ 2012?**
- **TP400-D6**
- **CR 8 Bld composite props**
- **Composite Wings & Emp**
- **Cruise M0.72 (300Kt)**
- **Ceiling > 37,000 ft.**
- **Range ~ 3000 nmi.**



# TP-400-D6

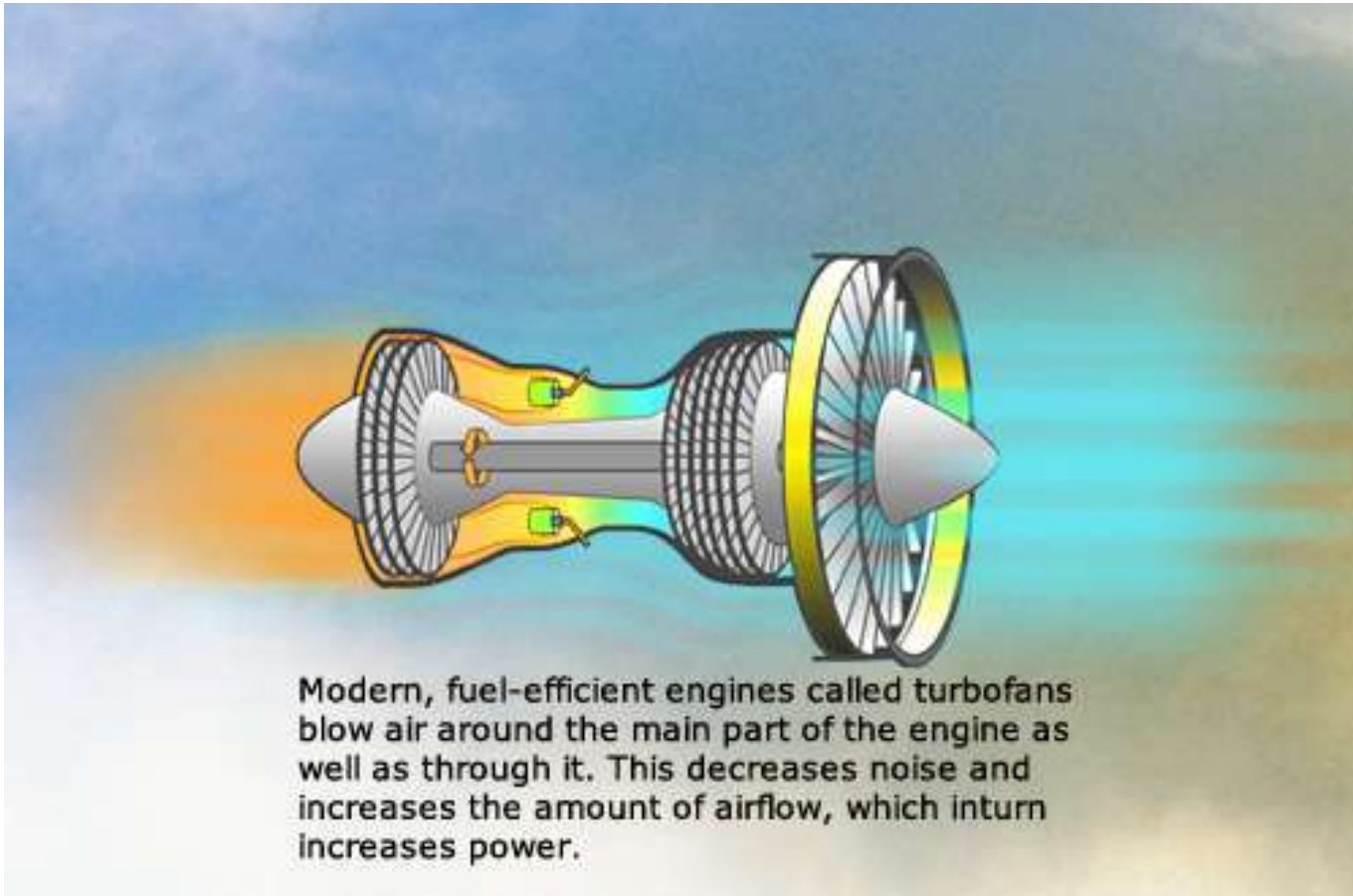
- 11,000 shp (8,200 Kw)
- 1,900 Kg
- TIT = 1500K
- 8 Bld CP composite prop
- Scimitar Propellers
- SFC = 0.4 lb/shp-hr
- Pwr/Wt = 4.4 Kw/Kg
- FADEC to Civil specs
- FOC 2009



**FADEC= Full Authority Digital Engine (or Electronic) Control**

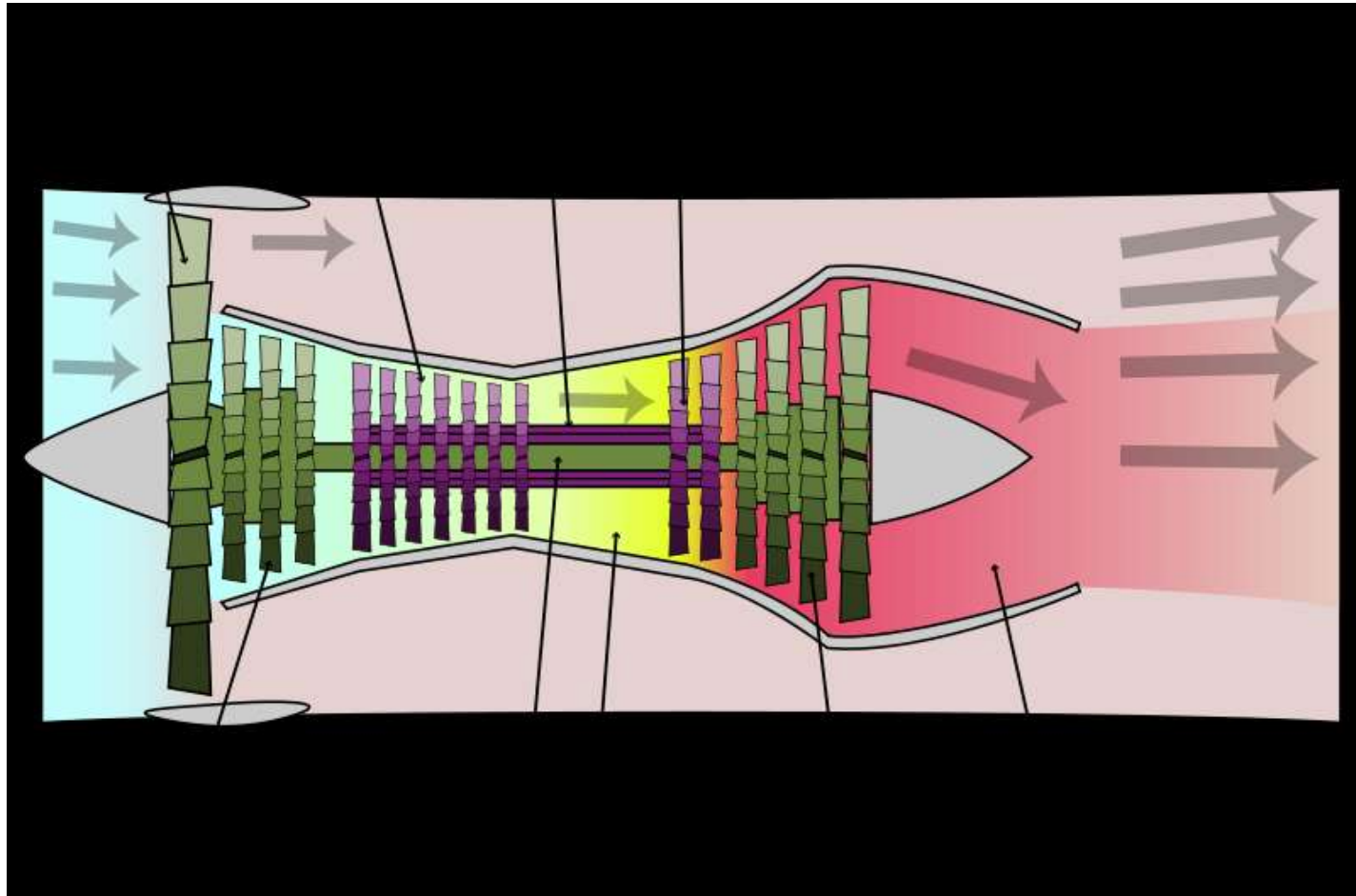
# Basic Turbofan Engine

High BPR increases Thrust Efficiency  
Large Air flow Mass at Low  $dv$

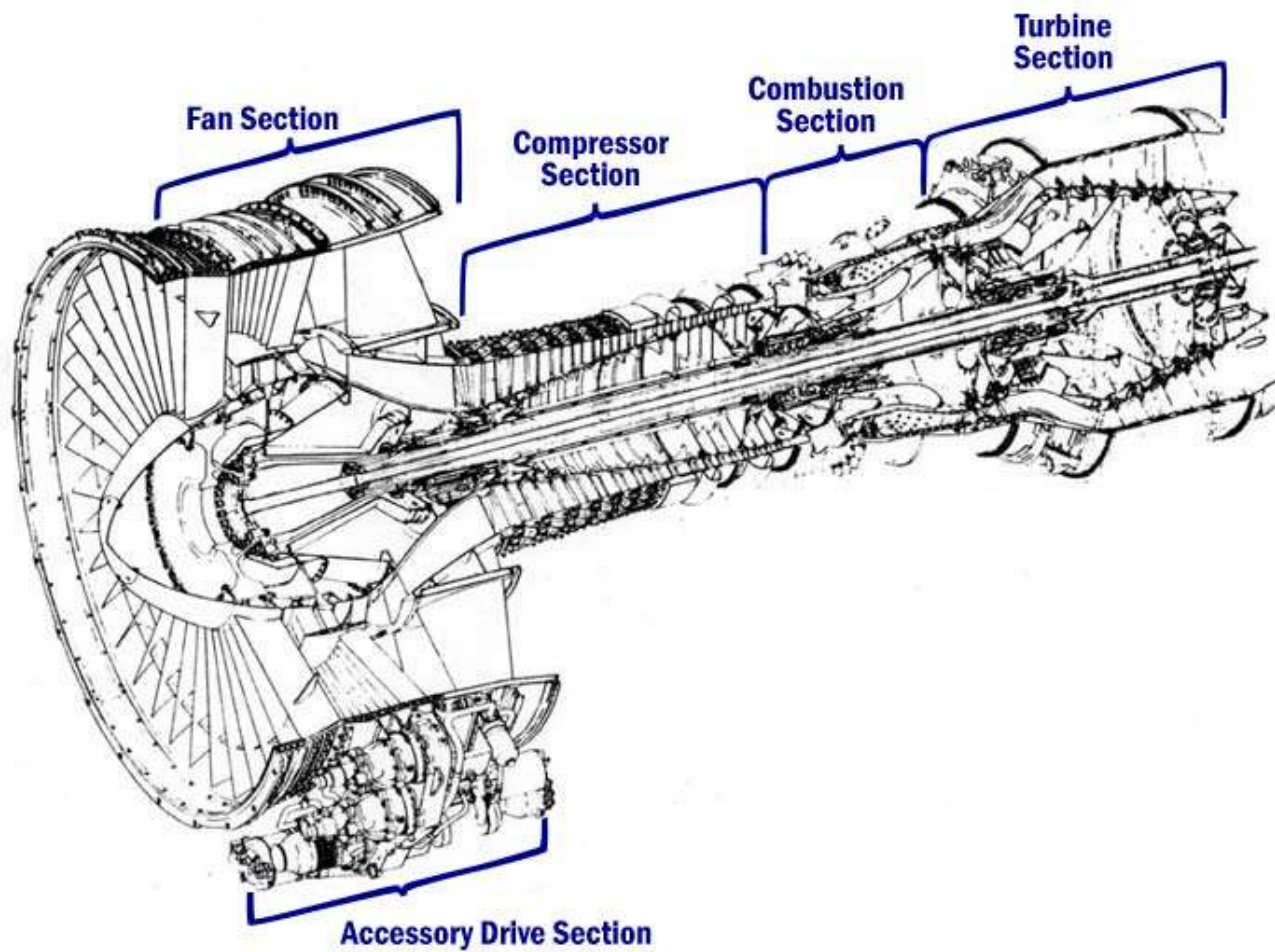




# High-bypass Turbofan



# GE CF6-6



# Some Typ. Long Range Turbo Fan Jets

| A/C                    | Engine        | Thrust<br>(KN) | Weight<br>(Kg) | BPR   |
|------------------------|---------------|----------------|----------------|-------|
| B 737-500/A320,A340    | CFM 56        | 100            | 1,950          | 6:1   |
| B 777-200LR            | GE 90         | 417            | 7,550          | 9:1   |
| B 787,B747-8           | GEnx          | 300            | 5,816          | 9.5:1 |
| B787                   | RR Trent 1000 | 330            | 5,765          | 11:1  |
| B747-400,767,A300,A310 | CF6-80C2      | 280            | 4,100          | 5.2   |

- GE90 has a 128 inch fan diameter

# Fanjet Commuter Aircraft

| A/C            | Engine     | Thrust (KN) | Weight (Kg) | BPR   |
|----------------|------------|-------------|-------------|-------|
| A318           | PW6000     | 100         | 2,289       | 5:1   |
| CRJ100/440     | GE CF 34-3 | 41          | 760         | 6.2:1 |
| E190/195,ARJ21 | GE CF34-10 | 89          | 1,700       | 5.1:1 |
| B717-200       | BR 715     | 83-95       | 2,800       | 4:1?  |
| G V            | BR 710     | 66          | 2,100       | ?     |

- BR 715 has a 58 inch fan diameter
- GE CF34-10 has a 57 inch total diameter

# **Some Final Thoughts**

- **BPR on Commuter Jets have been ~ 4 to 6:1**
- **Long Range, high efficiency engines have moved BPR ~ 9 to 11:1**
- **Q400 may be the future of Hub feeder routes**
- **Jet A fuel can be replaced by Synfuel at a cost of over ~\$60/bl**
- **Electric Propulsion is not in the future due to low energy density of source and high weight of engines**